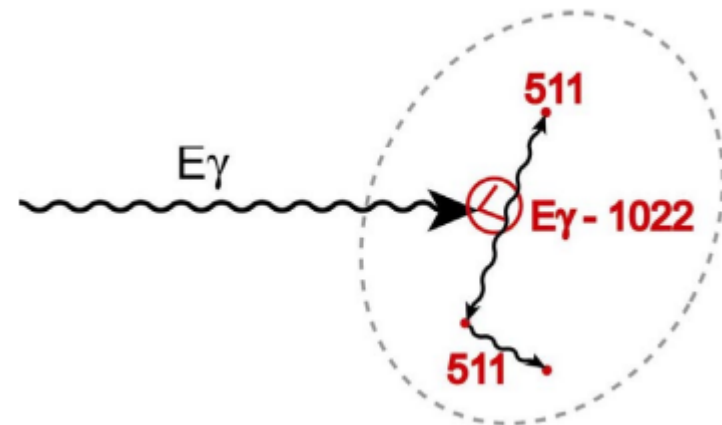


# Future of tracking

- Our examples follows
- 
- 
- 
- Hopefully you will have new ideas too

# Pair production

- Starts to dominate over  $\sim 9\text{MeV}$
- None of the codes we use now has this process included. Well, MGT has an approximation...
- *This would be a good research project!*  
***Machine Learning (ML) maybe?***, *pattern recognition?*
- Can produce single and double escape peaks



Best discussion I know of is in:  
evince [~/d6/epapers/Agata-proposal.pdf](#)

# Some other FOM measures

$$FOM = \frac{\sqrt{\sum_i^N [\cos(\theta_i^{theo}) - \cos(\theta_i)]^2}}{N-1} \quad \text{Dirk}$$

$$\chi^2 \sim \sum_{n=1}^{N-1} W_n \left( \frac{E_{\gamma'} - E_{\gamma}^{pos}}{E_{\gamma}} \right)_n^2 \quad \text{MGT}$$

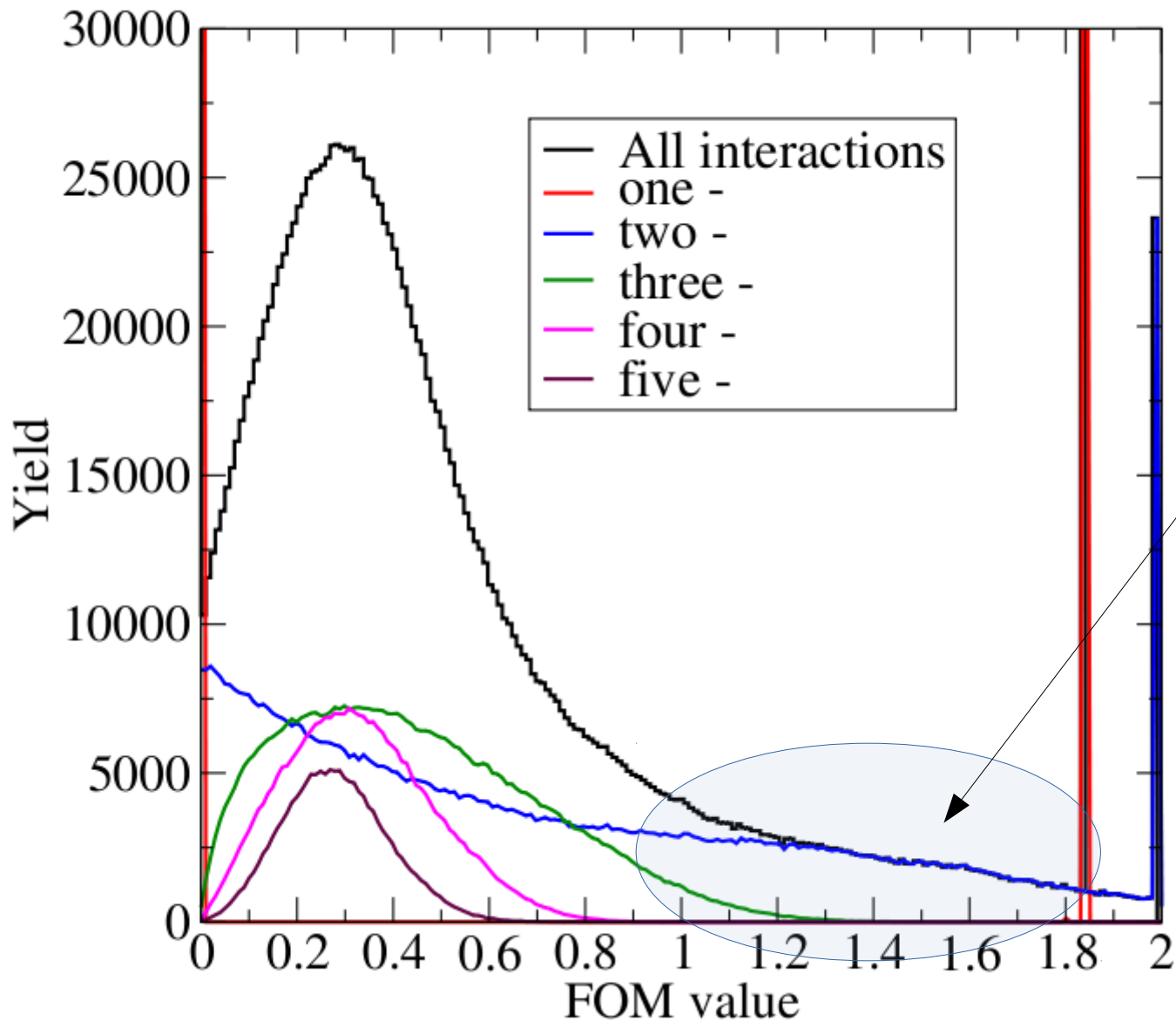
$$F_E = \exp\left(\frac{-2(E_{s,p} - E_{s,e})^2}{\sigma^2}\right) \quad \text{OFT (in some versions)}$$

$$w_1^{tot} = \frac{1}{N-1} \sum_{i=1}^{N-1} w_i^{step}$$

$$w_2^{tot} = \sqrt[N-1]{\prod_{i=1}^{N-1} w_i^{step}}$$

with :  $w_i^{step} \sim |\theta^{en} - \theta^{pos}|$

L. Milechina and B. Cederwall. *Nucl. Instrum. Methods. A*, 508:394, 2003.



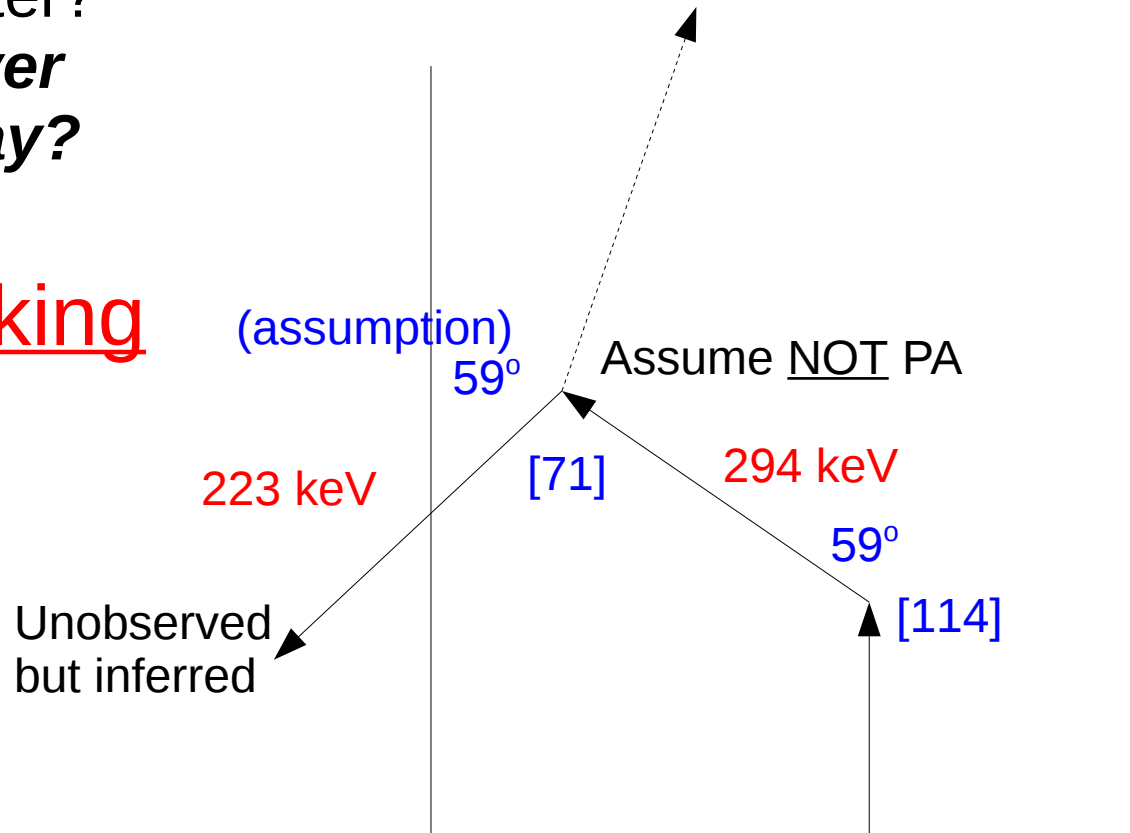
Many of these gamma rays, that are counted as gamma rays with two interactions and bad FOM, might be recovered using the TANGO tracking method if the loss of energy resolution can be tolerated

Probably worth adding a TANGO tracking option to the GT tracking code (TBD)

S. Tashenov and J. Gerl. Nucl. Instrum. Methods. A, 622:592, 2010.

Can we do better?  
**Can we recover  
 the gamma ray?**

**Maybe:  
TANGO tracking**



$$E_{\gamma} = \frac{E_{dep} + \sqrt{E_{dep}^2 + 4E_{dep}m_0c^2/(1 - \cos(\theta))}}{2} \rightarrow 408 \text{ KeV}$$

FOM= sqrt{ ==0 +0.0061}/(3-1) = 0.04  
 Accept as a good TANGO reconstructed energy

Energy and position uncertainty gives uncertainty to gamma ray energy  
 We cannot rescale to CC energy because CC did not see all the charge  
 For some experiments it may be good enough

# Add some internal range checking in the GT tracking code?

- As of now, there is no range checking in the GT tracking (apart from for single interactions)
- Maybe it would be good to check that the scattering length in the cluster with the lowest FOM does not have scatterings over ~4cm or so [make it a variable and optimize].
- If that is the case, **place a penalty on that particular scattering sequence**

# Appendix B: improving FOM calculation

- Would really like to propagate the errors on  $x, y, z, e$
- However, we know the errors are probably small for interaction that deposit a lot of energy and large for interactions with small deposited energies
- We suggest a new tracking formula with weights:

# Proposed new GT FOM measure

$$FOM = \frac{\sqrt{\sum_i w_i (\theta_i^{Compton} - \theta_i^{obs})^2}}{n_i - 1}; n_i > 1$$

$$w_i = \frac{E_{dep}^i}{E_{total}}$$

$$E_{total} = \sum_i E_{dep}^i$$



# Appendix: Including the “Compton profile”

$$\begin{aligned} \cos\theta = 1 - mc^2 \left( \frac{1}{E'_\gamma} - \frac{1}{E_\gamma} \right) \\ - \frac{1}{E_\gamma E'_\gamma} (Q^2 c^2 - Qc \{ Q^2 c^2 \\ + 2mc^2(E_\gamma - E'_\gamma) + (E_\gamma + E'_\gamma)^2 \}^{\frac{1}{2}}) \end{aligned} \quad (15)$$

Q==0 gives  
old formula

where

$$Q = \frac{E_\gamma E'_\gamma (1 - \cos\theta) - mc^2 (E_\gamma - E'_\gamma)}{c^2 \Delta p_\gamma} \quad (16)$$

Here  $c^2 \Delta p_\gamma$  is the absolute value of the momentum transfer and it can be written as

$$c^2 \Delta p_\gamma = \left( \frac{1}{c} \right) \{ (E_\gamma + E'_\gamma)^2 + 2E_\gamma E'_\gamma (1 - \cos\theta) \}^{\frac{1}{2}} \quad (17)$$

None of our  
tracking codes or  
GEANT4  
simulators include  
this effect (yet...)

J. van der Marel and B. Cederwall. Nucl. Instrum. Methods. A, 477:391, 2002.

M. J Cooper. Rep. Prog. Phys., 48:415, 1985.

# Remove some low energy interactions?

- We think that the decomposition gives us some 'extra' points
- They are possibly low energy
- We should try throwing away the low energy interaction in a cluster if the FOM was bad. See what the FOM is if we track without this interaction point

# Scattering angle checking in the GT tracking code?

- We currently accept all angles when we make permutations.
- Maybe we should penalize when an angle is less than  $\sim 20\%$  (make it a variable) probably according to the Klein-Nishina formula

## Appendix: catching long range scatter events

- Is it possible to catch gamma rays that Compton scatter from one side of the tracking array to the other?
- First scatter probably a single interaction that does not deposit much energy, i.e., the scattered gamma ray is energetic. How likely is this? *It is not likely...* backward scatters have scattered gamma rays with little energy to travel far...
- More likely to find such events in a cone of crystals that are not too far away.